



# Effect of floating bridge vertical motion on vehicle ride comfort and road grip

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# GOALS OF INVESTIGATION



Investigate the influence and analyze the effects of floating bridge vertical motion on:

- vehicle ride comfort and
- vertical force between wheel and ground.

# STEPS OF ANALYSIS

- **INPUTS**

Road roughness (stationary ground),  
Bridge vertical motion (moving ground).

- **VEHICLE MODEL**

Bus model (one dimensional 3 Degrees Of Freedom).

- **OUTPUTS**

Vertical driver's acceleration (weighted *RMS* value),  
Vertical force (Dynamic Load Coefficient – *DLC*).

# DISTURBANCES FROM STATIONARY GROUND

- Road roughness – very good/good condition  
(class A/B – ISO 8608 standard)

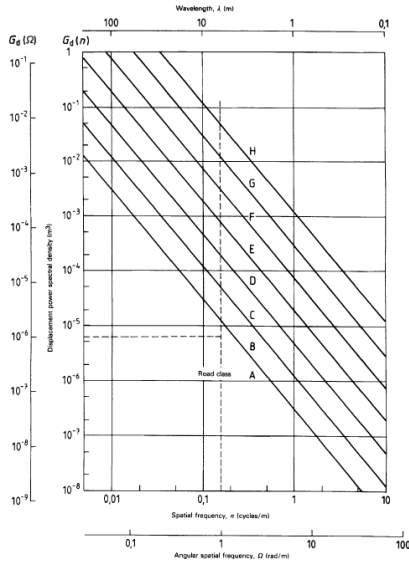
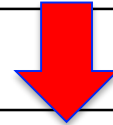


Figure C.2 – Classification of roads

$$\Phi_{\xi}(n) = \Phi_{\xi}(n_0) \cdot \left(\frac{n}{n_0}\right)^{-w}$$

$$\zeta(x) = \sum_{i=1}^N A_i \cos(n_i x - \alpha_i)$$

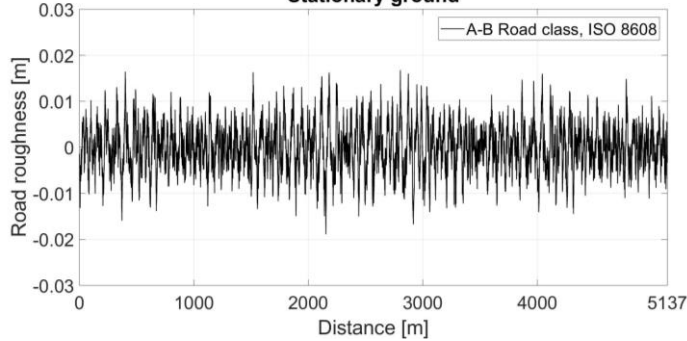
Power  
Spectral  
Density



Road  
Roughness

# Road roughness modelling (class A/B – ISO 8608)

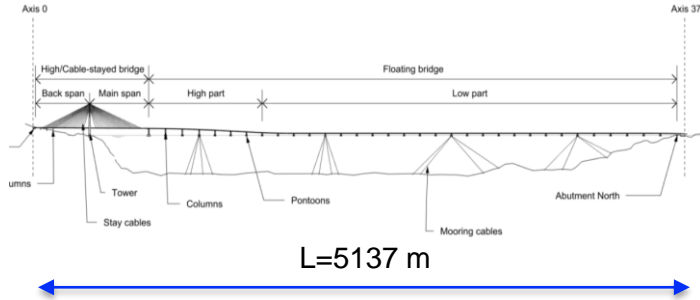
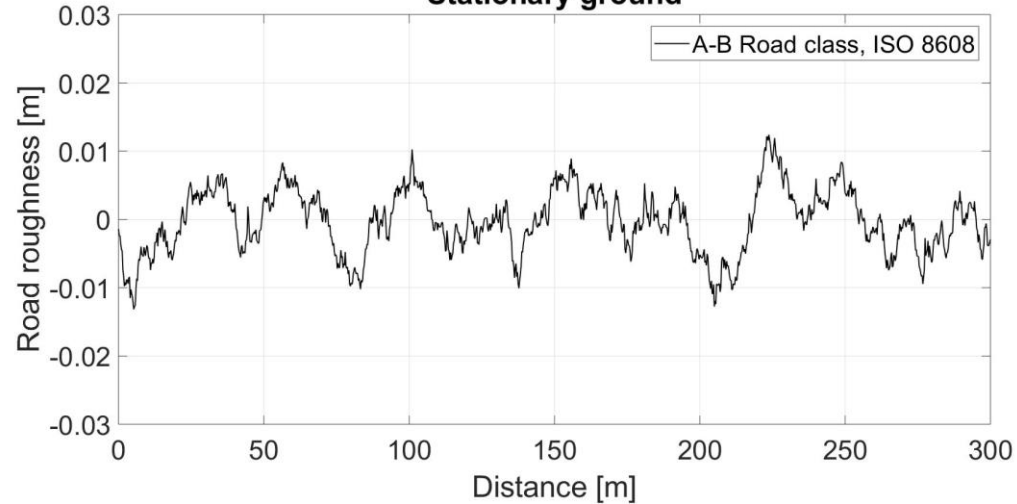
Stationary ground



Distance equal to  
bridge length,  $L=5137$  m.

Road roughness sample  
(length of 300 m).

Stationary ground



**Bjørnafjorden, straight floating bridge**

# DISTURBANCES FROM MOVING GROUND

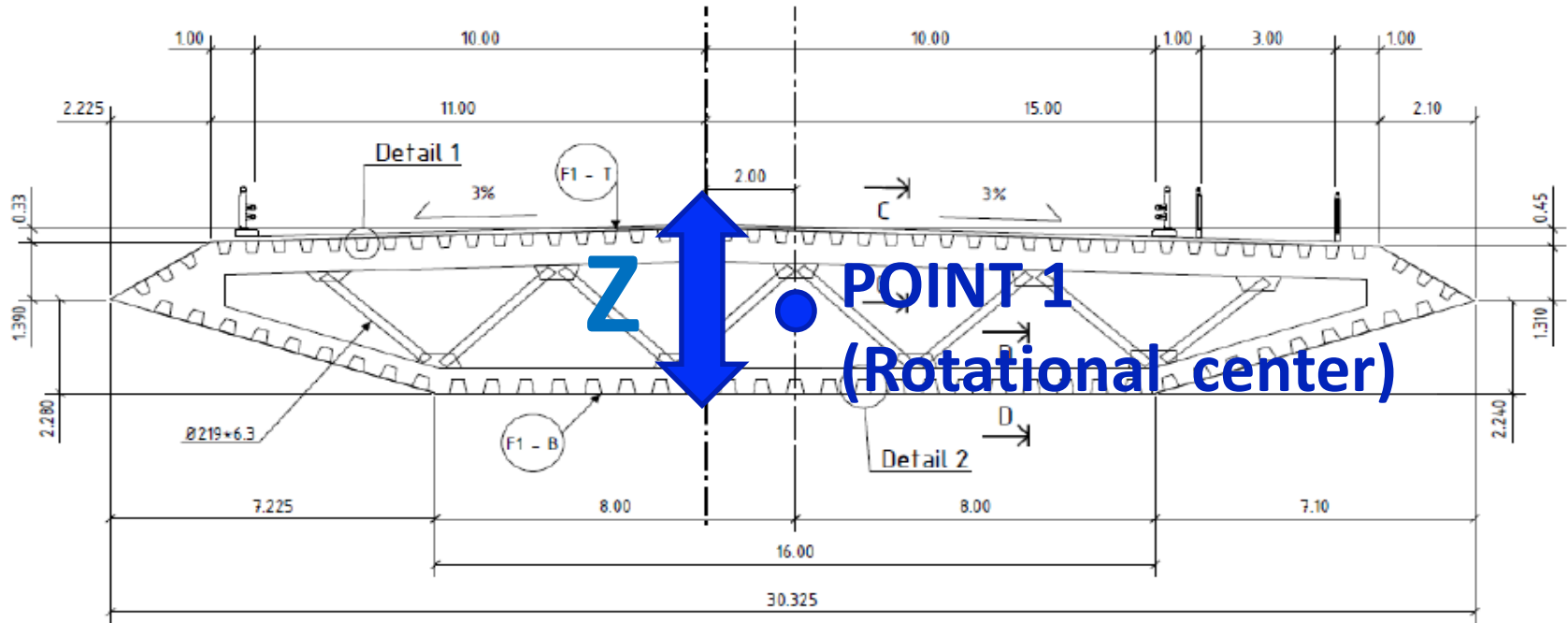
Two common approaches on bridge-vehicle interaction:

- (1) bridge-vehicle interaction that refers to the mechanism where bridge vibration is due to vehicle movement and vehicle vibration is due to bridge movement (coupling system) and
- **(2) bridge-vehicle interaction that refers to the mechanism where vehicle vibration is due to input from bridge vibration.**

# DISTURBANCES FROM MOVING GROUND

- In this study, vehicle mass is negligible compared to mass of the bridge. This means vehicle motion does not significantly affect bridge vibration (Siringoringo et al, 2012).
- Vertical bridge displacements input to the vehicle obtained from the actual displacements according to the **time and location** of vehicle's wheels contact with the bridge deck.

# Vertical bridge motion (up and dawn, z-direction)



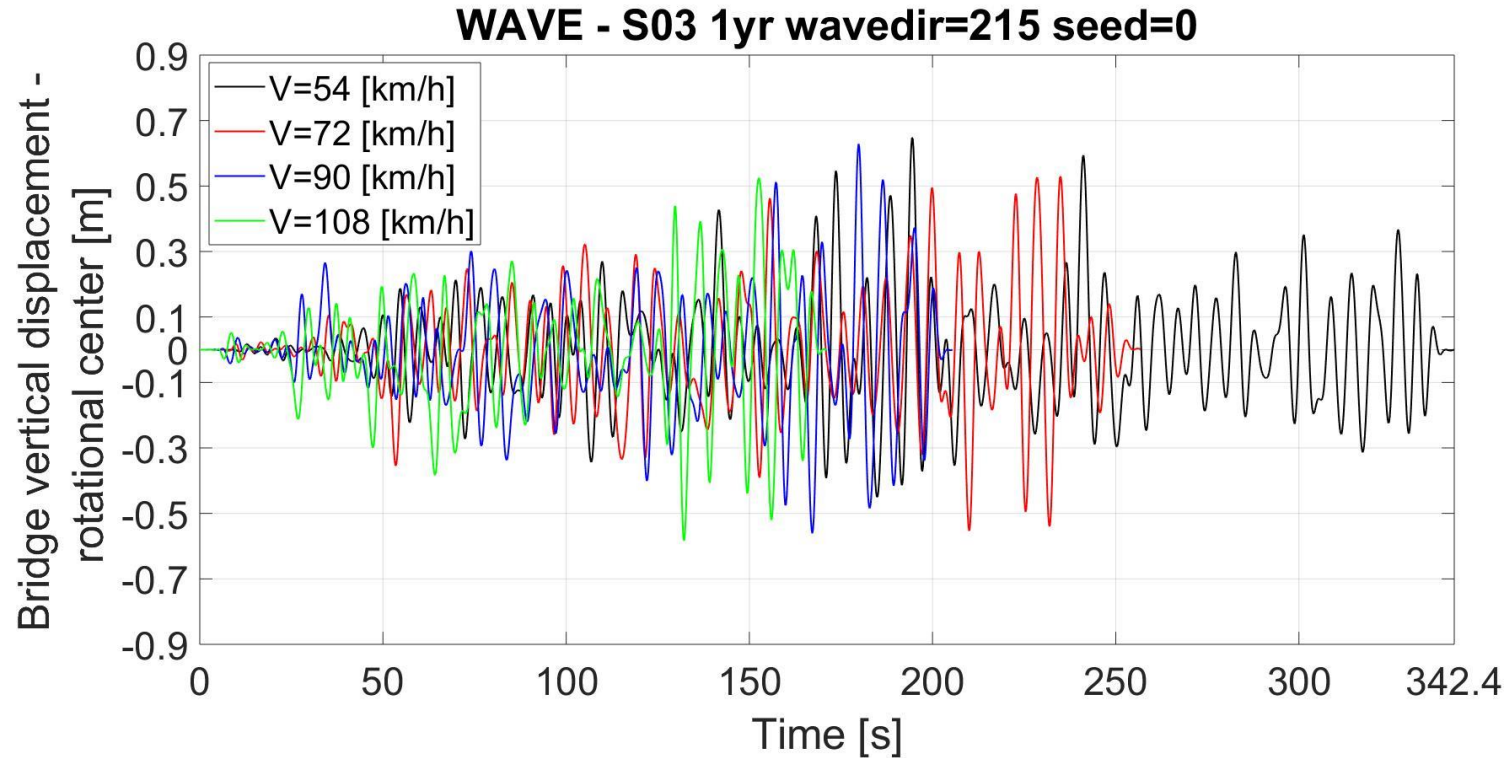
**Cross section of the bridge deck**



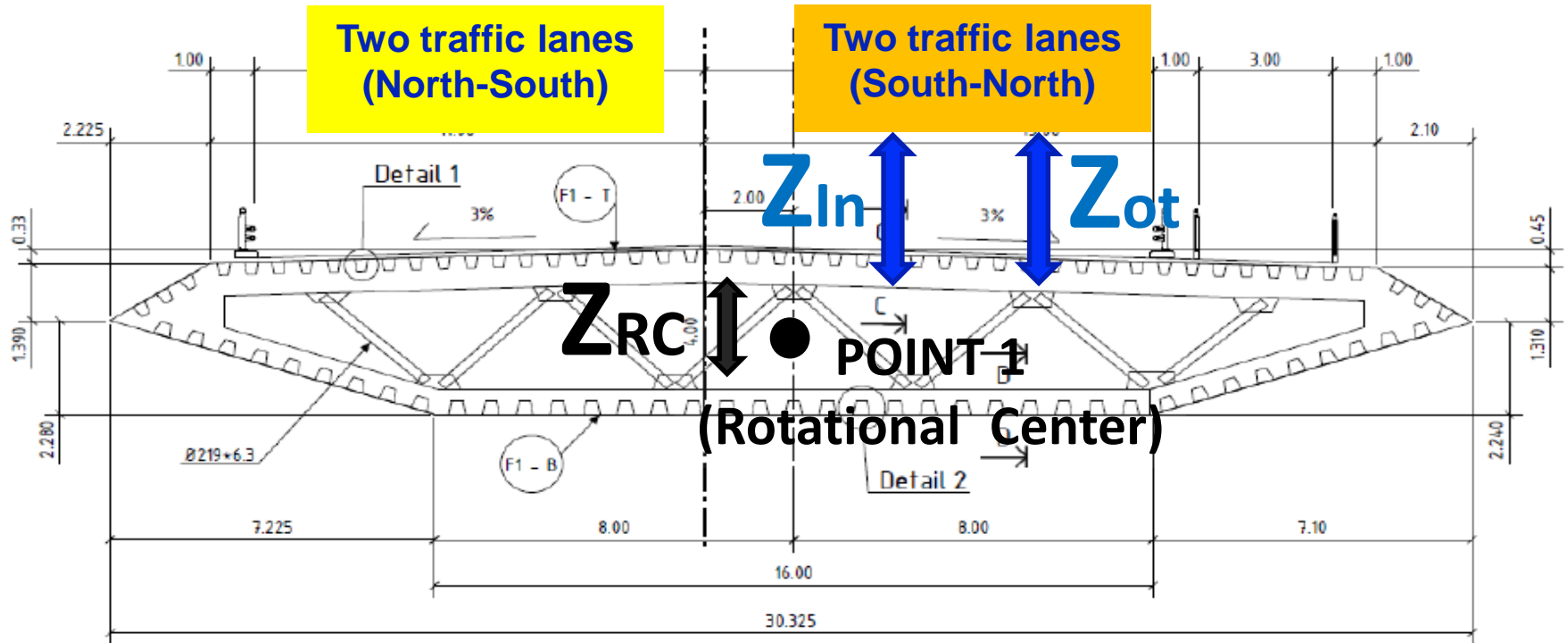
# Different 1-year storm conditions

- (I) 1 year response, wave only, wave direction 100 deg (from east);
- (II) 1 year response, wave only, wave direction 215 deg (325 global, from North West);
- (III) 1 year response, wind only, wind direction 90 (from east);
- (IV) 1 year response, wind only, wind direction 270 deg (from west);
- (V) 1 year response, **all loads**, wave + wind [ (I) + (III) ]
- (VI) 1 year response, **all loads**, wave + wind [ (II) + (IV) ]

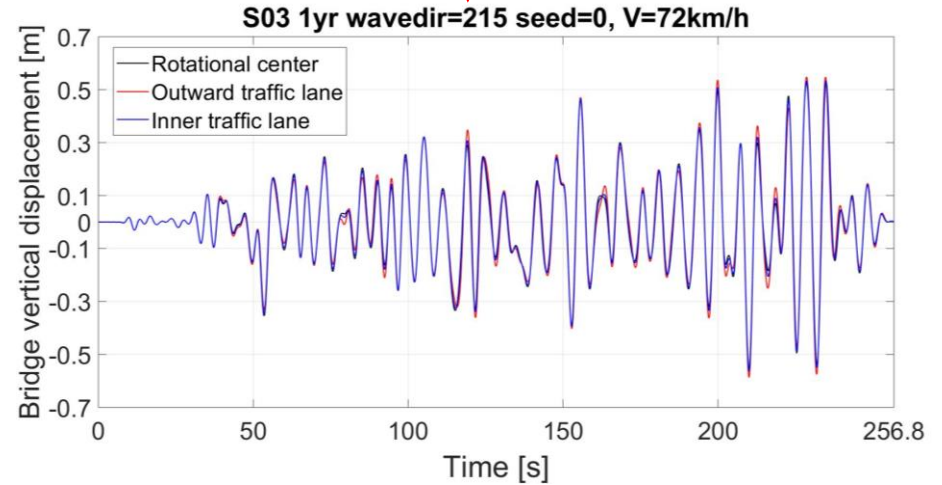
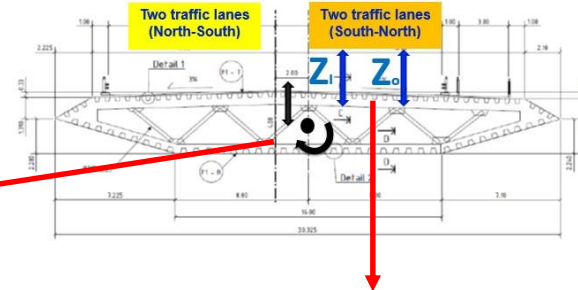
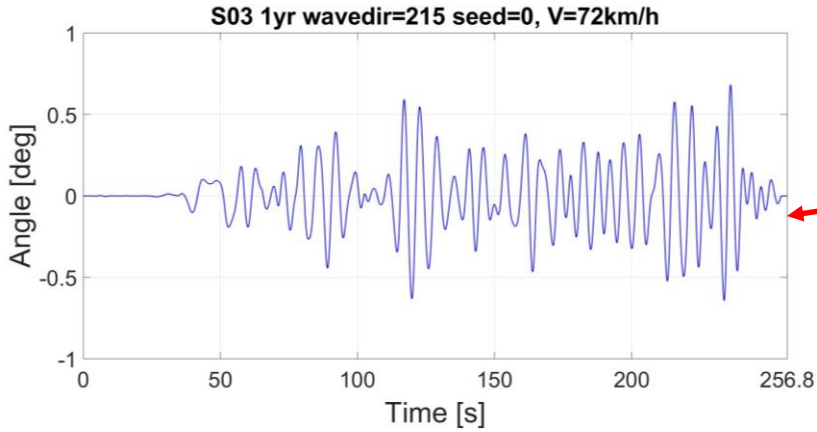
# Vertical motion along the bridge due to wave load



# Vertical motions for different traffic lanes

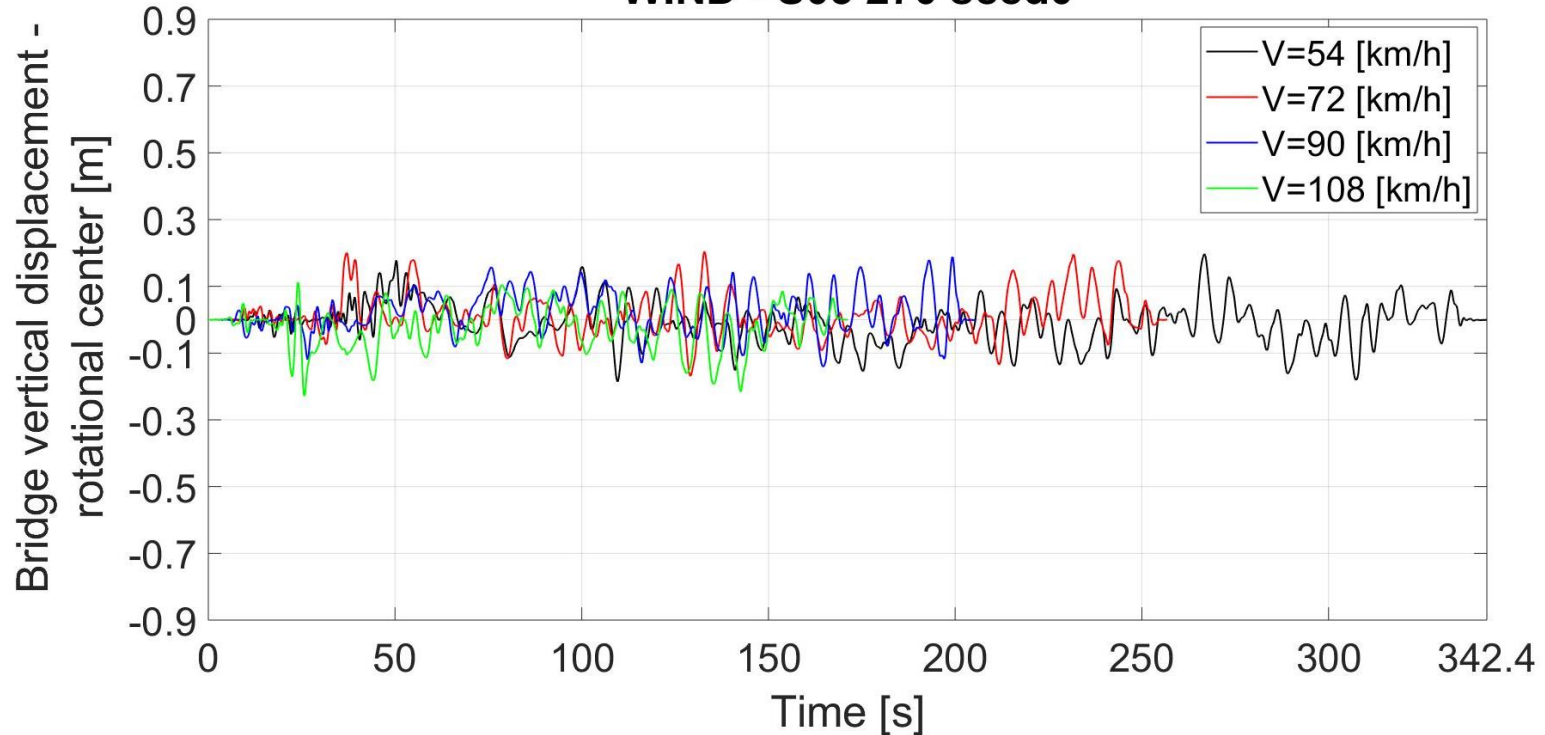


# Vertical motions for two different traffic lanes

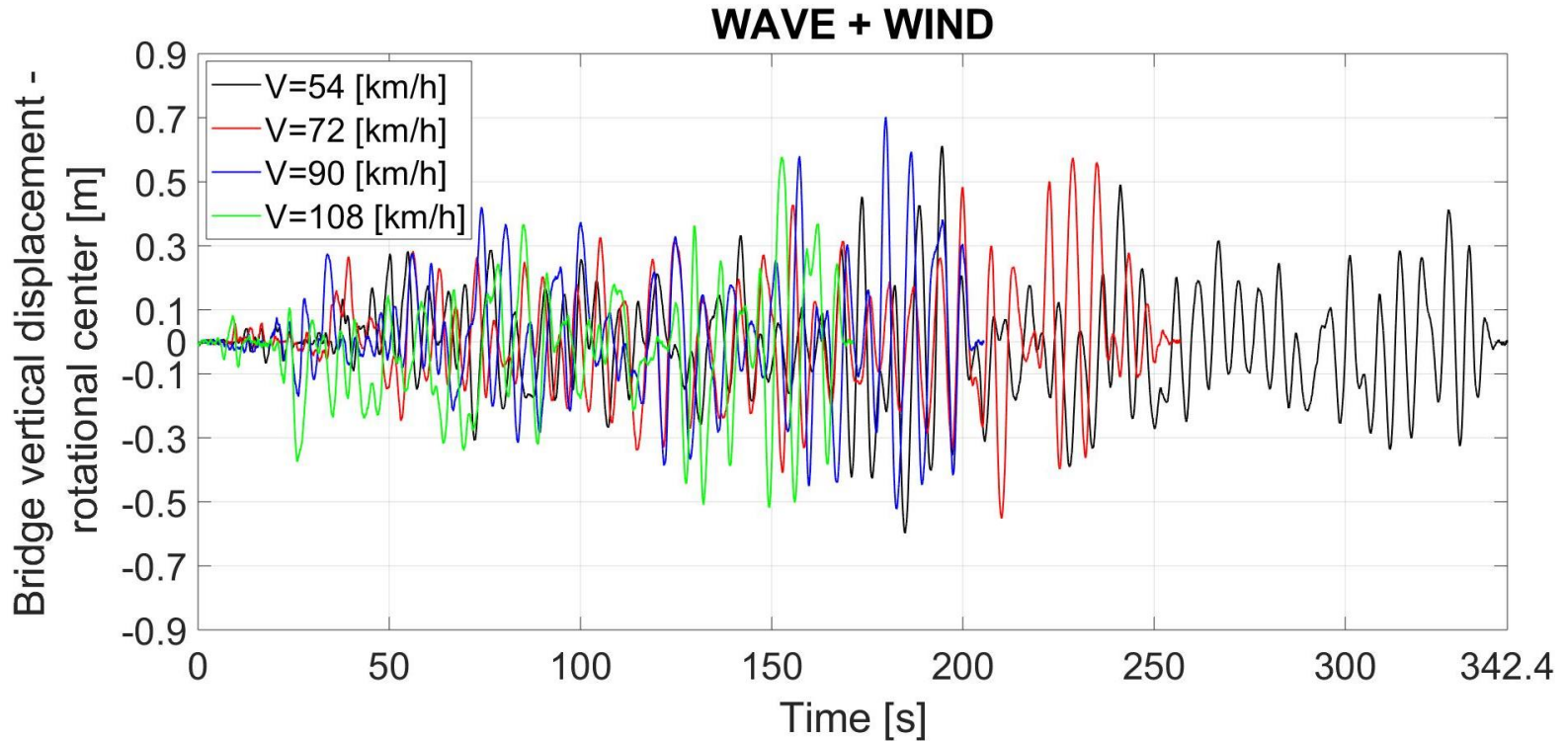


# Vertical motion along the bridge due to wind load

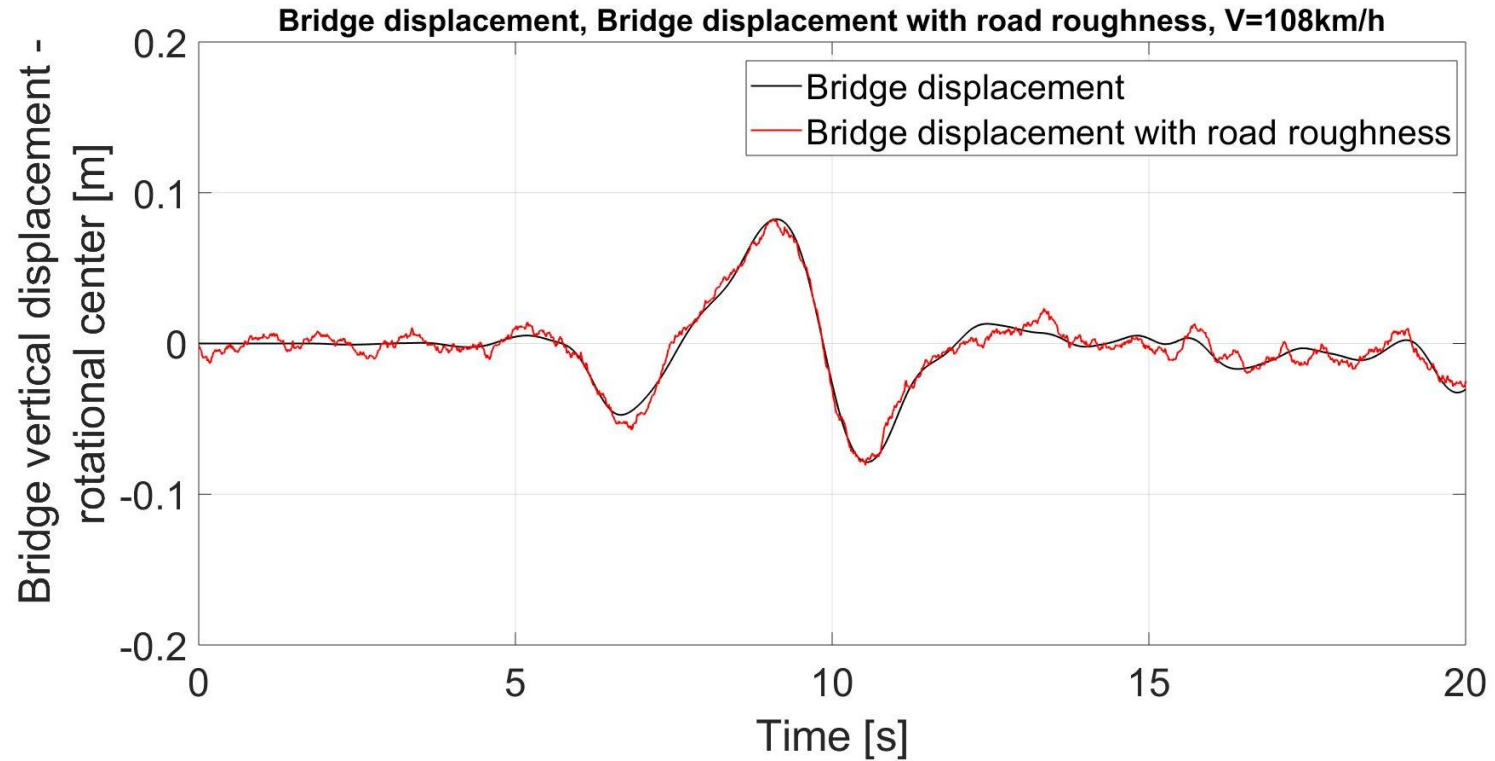
WIND - S03 270 seed0



# Vertical motion along the bridge due to wind and wave loads

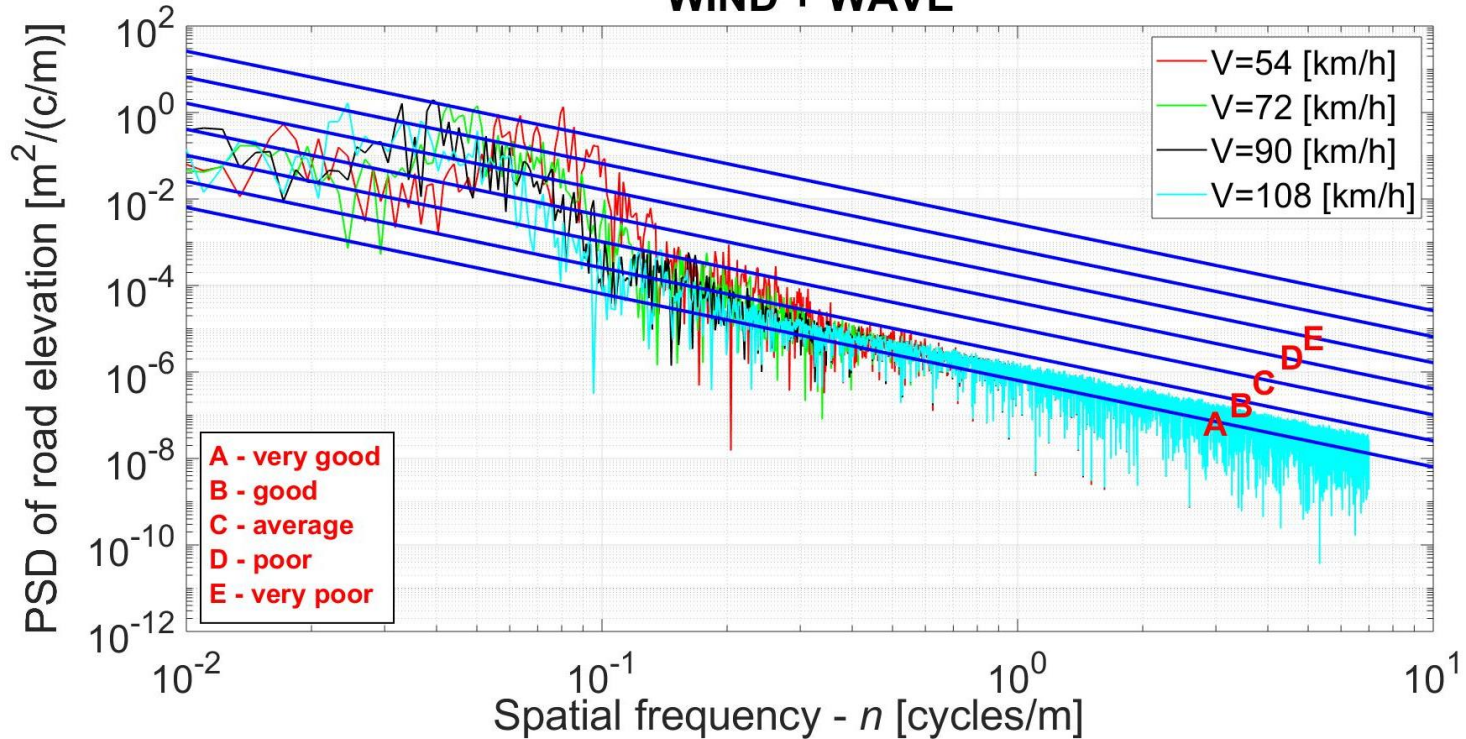


# Bridge displacement and road roughness – model input



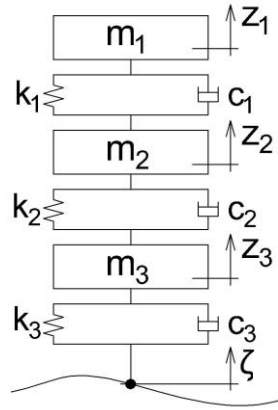
# Bridge displacement as road roughness in ISO 8608

WIND + WAVE





# BUS MODEL – one dimensional 3 Degrees Of Freedom



## Differential equations of motion:

$$m_1 \ddot{z}_1 + c_1 \dot{z}_1 + k_1 z_1 - c_1 \dot{z}_2 - k_1 z_2 = 0$$

$$m_2 \ddot{z}_2 + (c_1 + c_2) \dot{z}_2 + (k_1 + k_2) z_2 - c_1 \dot{z}_1 - k_1 z_1 - c_2 \dot{z}_3 - k_2 z_3 = 0$$

$$m_3 \ddot{z}_3 + (c_2 + c_3) \dot{z}_3 + (k_2 + k_3) z_3 - c_2 \dot{z}_2 - k_2 z_2 = c_3 \dot{\zeta} + k_3 \zeta$$

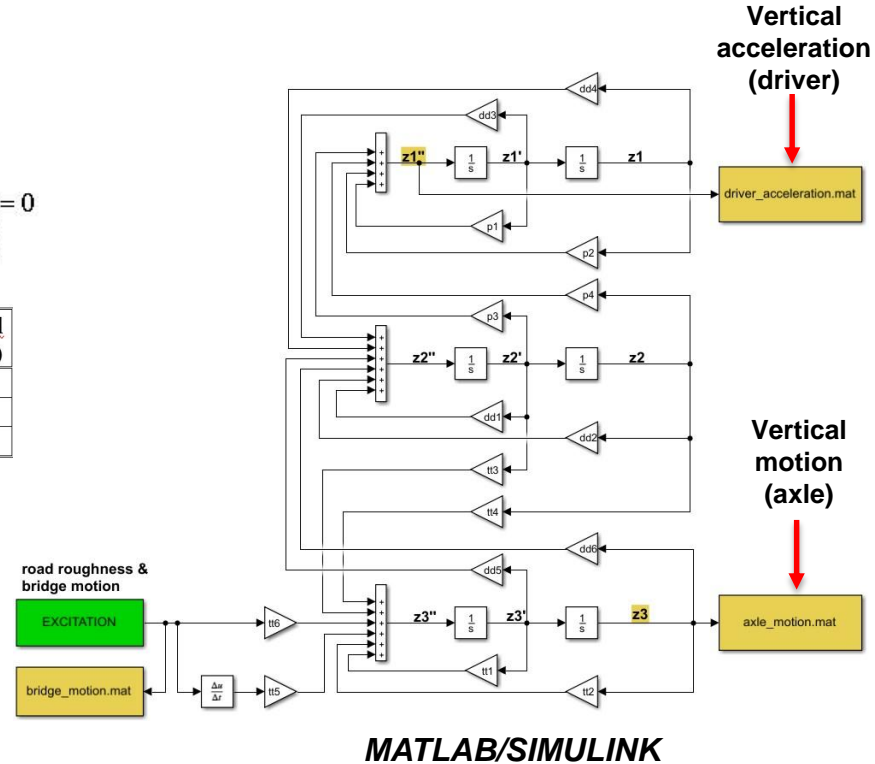
Concentrated mass	Undamped natural frequencies (Hz)	Damped natural frequencies (Hz)
Seat+driver - m1	2.2916	2.1403
Sprung mass - m2	1.2864	1.2790
Unsprung mass - m3	9.6174	9.4955

```
% BUS QUARTER MODEL PARAMETERS;
% mass parameters;
m1 = 100; % driver+seat [kg];
m2 = 4000; % sprung mass [kg];
m3 = 550; % unsprung mass [kg];
```

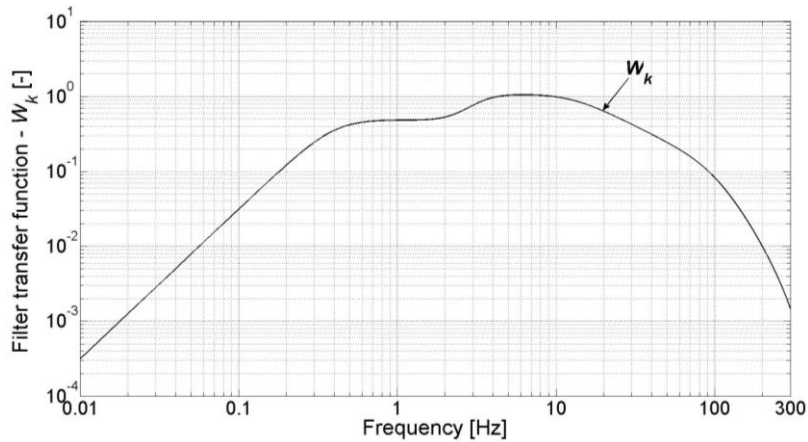
```
% oscillatory parameters;
k1 = 20000; % driver's seat suspension spring stiffness [N/m];
k2 = 320000; % suspension spring stiffness [N/m];
k3 = 1700000; % bus tyre radial stiffness [N/m];
```

```
c1 = 1000; % driver's seat shock absorber damping [Ns/m];
c2 = 10000; % suspension shock absorber damping [Ns/m];
c3 = 150; % wheel damping [Ns/m];
```

Bus data from Ref. (Agostinacchio et al.)



# VERTICAL WEIGHTED ACCELERATION – ISO 2631 (1997)



**Weighting filter -  $W_k$**

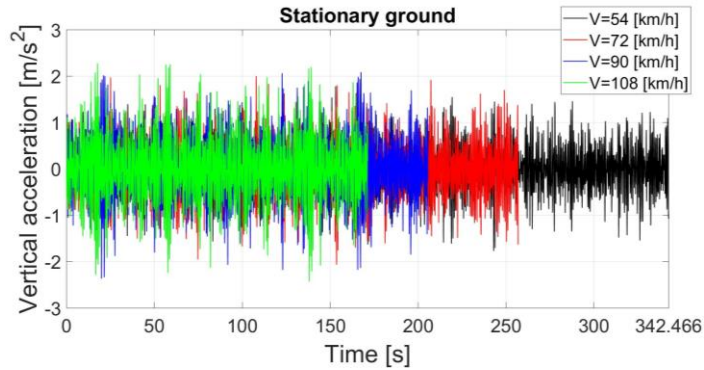


**ISO 2631 (1997) criteria**

$$\ddot{z}_{rms,w} = \sqrt{\frac{1}{T} \int_0^T \ddot{z}_w(t)^2 dt}$$

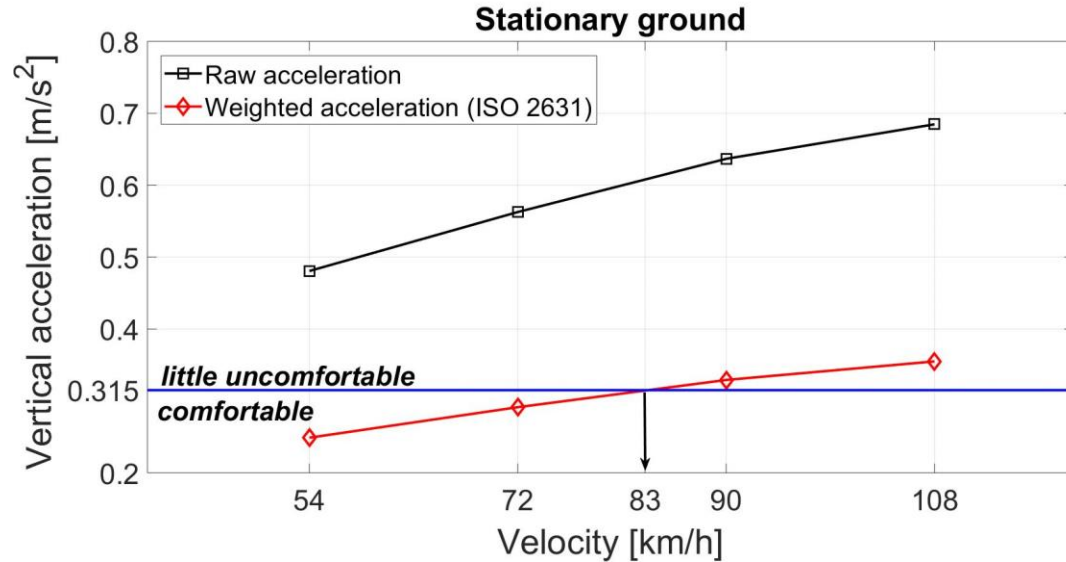
**RMS of the weighted vertical acceleration**

# Vertical driver's acceleration



Vertical acceleration

For bus speed above 83 km/h, driving is *'little uncomfortable'*.



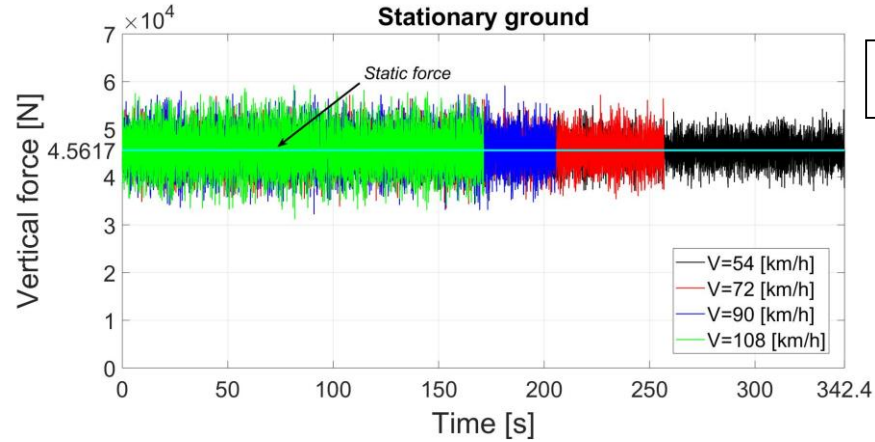
## Vertical force – Dynamic Load Coefficient

DLC represents ratio of standard deviation of total axle load (or *RMS* value of dynamic axle load) and static axle load.

$$DLC = \frac{\sigma_Z}{Z_{st}} = \frac{Z_{dyn,RMS}}{Z_{st}}$$

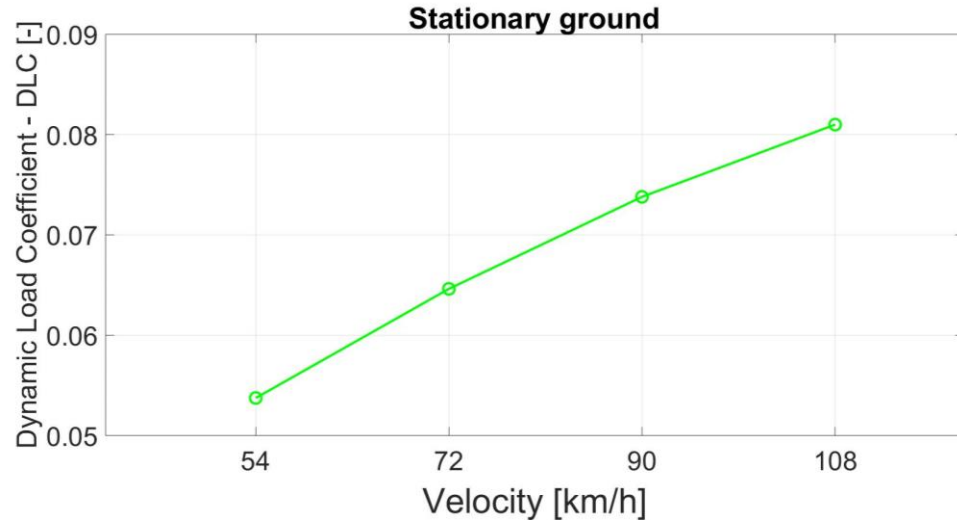
**Lower value of *DLC* points out better contact between wheel and road.**

# Vertical force – Dynamic Load Coefficient



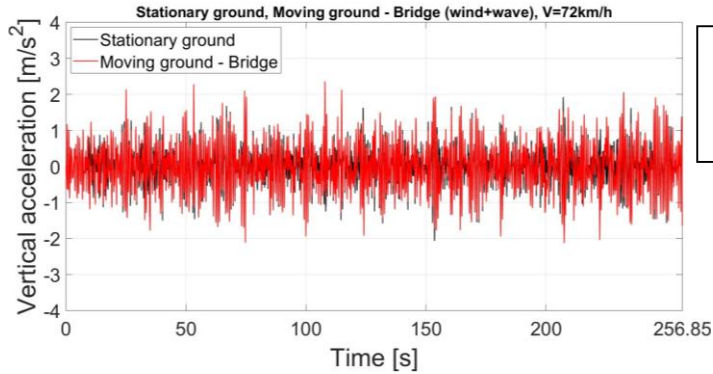
Vertical force

Dynamic Load Coefficient



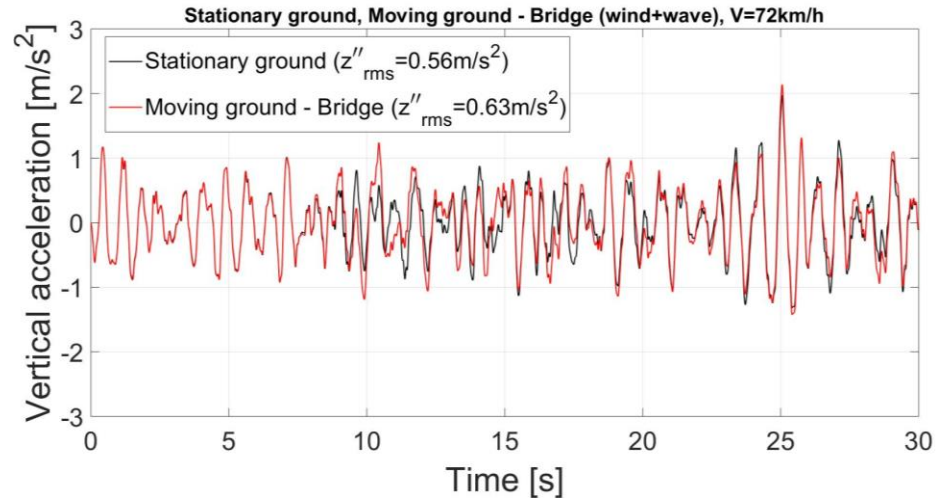
# COMPARASION OF BUS MODEL RESPONSES

- **Example of vertical raw acceleration of the driver**

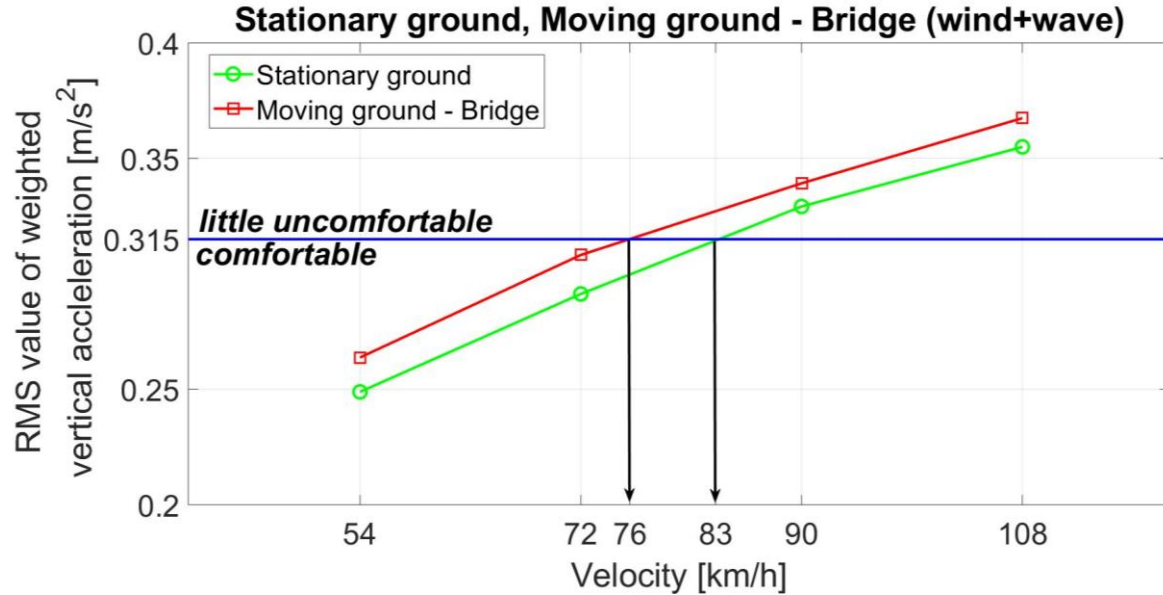


Vertical acceleration signal for bus speed of 72 km/h.

Vertical acceleration signal for 30 s.



# Weighted vertical acceleration of the driver

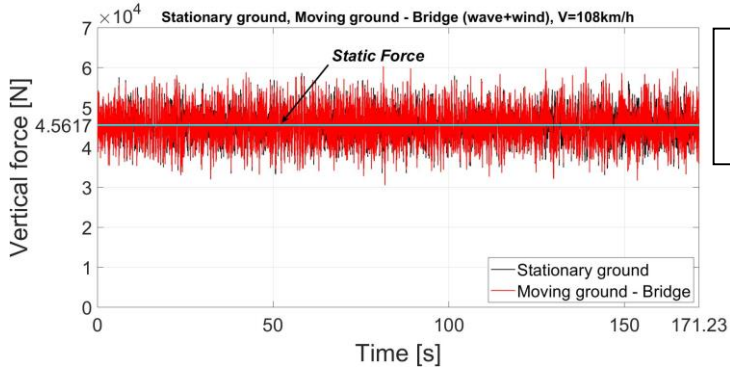


For bus speed above 83 km/h, driving is **'little uncomfortable'** for stationary ground.  
 For bus speed above 76 km/h, driving is **'little uncomfortable'** for moving ground - bridge.

**Speed decreases by 8.43 %.**

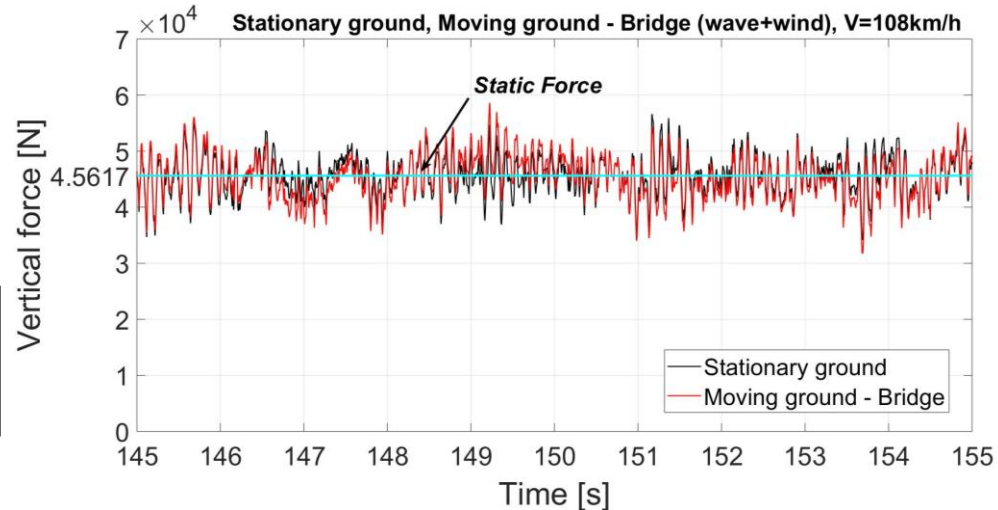
# COMPARASION OF BUS MODEL RESPONSES

- Example of vertical force



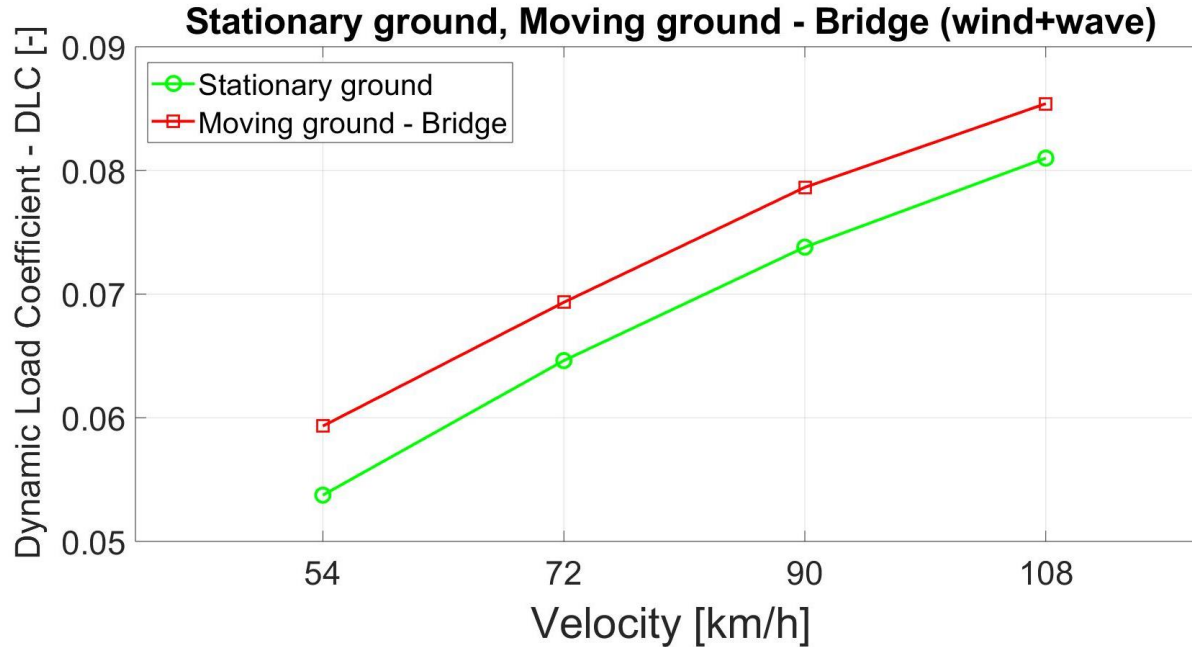
Vertical force signal for bus speed of 108 km/h.

Sample of vertical force signal for 145-155 s.





# Dynamic Load Coefficient

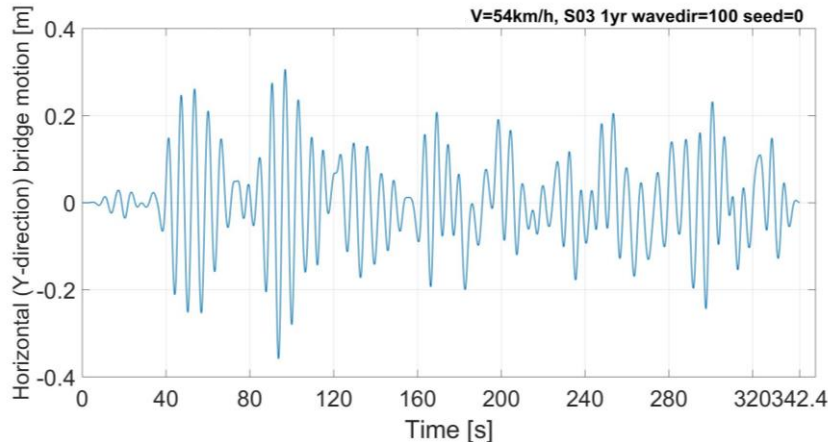


Higher values of  $DLC$  for the case of moving ground points out higher variation in vertical forces (lower road grip).

# FUTURE INVESTIGATION

Building complex model that can capture signals of lateral bridge motion and winds.

Investigate the influence of those loads on **lateral/vertical** vehicle behavior.



Signal of horizontal bridge motion (Y-direction).